

Algebra

Word Problems with Consecutive Integers/Variables on Both Sides

On a separate sheet of paper, do the following for each word problem: define the variable/unknowns, write an algebraic equation, solve using proper steps, and state the final answer in a complete sentence.

Consecutive Integers: {..., -3, -2, -1, 0, 1, 2, 3, ...}.

The three types of situations:

If n is defined as an integer, then the next two consecutive integers are $n+1$ and $n+2$

If n is defined as an even integer, then the next two consecutive even integers are

If n is defined as an odd integer, then the next two consecutive odd integers are $n+2$ and $n+4$

Example:

The sum of three consecutive even integers is 30 more than the largest.

n = smallest even integer

$n+2$ = middle even integer

$n+4$ = largest even integer

$$n + n + 2 + n + 4 = 30 + n + 4$$

$$3n + 6 = n + 34$$

$$\begin{array}{r} -n \quad -n \\ 2n + 6 = 34 \end{array}$$

$$\begin{array}{r} -6 \quad -6 \\ \underline{2n} = \underline{28} \end{array}$$

$$\begin{array}{r} \underline{2} \quad \underline{2} \\ n = 14 \end{array}$$

The three consecutive even integers are 14, 16, and 18.

- The sum of four consecutive integers is -42. What are the integers?
- The sum of four consecutive even integers is -100. What are the integers?
- Find three consecutive odd integers whose sum is 105.
- The sum of three consecutive odd integers is 40 more than the smallest. What are the integers?
- The greater of two consecutive even integers is six less than twice the smaller.
- The least of three consecutive odd integers is 2 more than half the largest. What are the integers?
- The lengths of the sides of a triangle are consecutive even integers. Find the length of the longest side if it is 22 cm shorter than the perimeter.
- Cingular Wireless offers a cell phone plan that costs \$49.99 per month. Verizon Wireless offers a plan that costs \$54.99 per month. With Cingular, additional minutes cost \$0.40 and with Verizon additional minutes cost \$0.35. How many additional minutes will it take for a monthly bill from Cingular to be the same as Verizon?
- The cost to purchase a song from iTunes is \$0.99 per song. To purchase a song from Napster, you must be a member. The Napster membership fee is \$10. In addition, each purchased song costs \$0.89. How many songs must be purchased so that the costs are the same?
- A family has three options for a child's birthday party: Adventure Plex, Bright Child, and Chuck E. Cheese. At Adventure Plex, there is a flat fee of \$300, each child costs \$12. At Bright Child, there is a \$180 flat fee, each child costs \$15. At Chuck E. Cheese, there is not flat fee, but each child costs \$18.
 - Determine the breakeven point for Adventure Plex and Bright Child.
 - Determine the breakeven point for Adventure Plex and Chuck E. Cheese.
 - Determine the breakeven point for Bright Child and Chuck E. Cheese.
- Homer Simpson weighs 400 pounds. He is on a diet to lose 5 pounds each week. Barney Gumble weighs 322 pounds. He is on a diet to lose 3 pounds each week. How long will it take for them to weigh the same?
- The Comic Book Guy weighs 435 pounds and is on a diet to lose five pounds each week. Professor Frink weighs 123 pounds and is on a diet to gain three pounds each week. How long will it take for them to weigh the same?
- At McDonald's, the barbecue sauce packet has five fewer calories than the sweet-n-sour sauce packet. Ten barbecue sauce packets have the same amount of calories as nine sweet-n-sour sauce packets. How many calories does each have?
- A 2000L tank containing 550L of water is being filled with water at the rate of 75L/minute from a full 1600L tank. How long will it be before the two tanks have the same amount of water?
- Bart has two choices to make a long distance phone call. His two choices are: 10-10-220 and AT&T. Using 10-10-220, the cost is 99¢ for the first twenty minutes, and 7¢ for each additional minute. AT&T just charges 6¢ for each minute. After how many total minutes will it be less expensive to use AT&T? Assume the call is at least 20 minutes.
- Your family is moving into a new home. Rather than do the work yourselves, you get price quotes from two different moving companies. Starving Students Movers charges \$100 for the first hour and \$50 for subsequent hours. Allied Movers charges \$60 for each hour. After how many hours will it be more advantageous to have Starving Student move your families' junk?